

# The Loss of Adaptive Plasticity during Long Periods of Environmental Stasis

Joanna Masel,<sup>1,\*</sup> Oliver D. King,<sup>2,†</sup> and Heather Maughan<sup>1,‡</sup>

1. Department of Ecology and Evolutionary Biology, University of Arizona, Tucson, Arizona 85721;

2. Whitehead Institute for Biomedical Research, Cambridge, Massachusetts 02142

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**ABSTRACT:** Adaptive plasticity allows populations to adjust rapidly to environmental change. If this is useful only rarely, plasticity may undergo mutational degradation and be lost from a population. We consider a population of constant size  $N$  undergoing loss of plasticity at functional mutation rate  $m$  and with selective advantage  $s$  associated with loss. Environmental change events occur at rate  $\theta$  per generation, killing all individuals that lack plasticity. The expected time until loss of plasticity in a fluctuating environment is always at least  $\bar{\tau}$ , the expected time until loss of plasticity in a static environment. When  $mN > 1$  and  $N\theta \gg 1$ , we find that plasticity will be maintained for an average of at least  $10^8$  generations in a single population, provided  $\bar{\tau} > 18/\theta$ . In a metapopulation, plasticity is retained under the more lenient condition  $\bar{\tau} > 1.3/\theta$ , irrespective of  $mN$ , for a modest number of demes. We calculate both exact and approximate solutions for  $\bar{\tau}$  and find that it is linearly dependent only on the logarithm of  $N$ , and so, surprisingly, both the population size and the number of demes in the metapopulation make little difference to the retention of plasticity. Instead,  $\bar{\tau}$  is dominated by the term  $1/(m + s/2)$ .

**Keywords:** population genetics, Moran model, fluctuating environment, phenotypic plasticity, regressive evolution.

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Some traits may be strongly adaptive but only on very rare occasions. This is typically true for plastic traits that are expressed only when the need arises. Such traits are particularly common in microbes, and there has been much interest recently in phenotypic switching behaviors as a response to novel and hostile environments (Henderson et al. 1999; Hallet 2001). Examples of potentially adaptive phenotypic switching include pili expression in bacteria (Abraham et al. 1985), phage growth limitation machinery (Sumbly and Smith 2003), bacterial persistence (Balaban et al. 2004; Kussell and Leibler 2005), the yeast prion [*PSI*<sup>+</sup>] (True and Lindquist 2000; Masel and Bergman 2003; Masel 2005), sporulation, and biofilm formation. Adaptive phenotypic plasticity is also common in multicellular organisms (West-Eberhard 2003).

The ability to undergo phenotypic switching is a complex trait in the sense that it is easy to lose by mutation but hard to gain back. Although the trait may be strongly adaptive under certain circumstances, these circumstances arise only rarely. The trait may be eroded and lost through mutational degradation during the potentially long gaps between times when the trait is needed. This is not an issue in an infinite population, in which traits are never lost but instead only become vanishingly rare. In a finite population, however, with restoration through compensatory mutation too rare to be significant, all complex but rarely needed traits will eventually be lost, given infinite time. What, then, accounts for their observed persistence? Here we develop an approach based on Markov models of finite populations to find the parameter range required for the expected time until trait loss to be sufficiently large (taken arbitrarily as  $>10^8$  generations) so that trait loss is effectively negligible on evolutionary timescales.

## Mathematical Model and Results

### *Trait Loss from a Single Population*

**Overall Approach.** Consider, for mathematical simplicity, a haploid population of size  $N$  under the Moran model; that is, at each time step, one individual is chosen at random to reproduce and one to die. One generation consists

\* E-mail: masel@u.arizona.edu.

† E-mail: oking@wi.mit.edu.

‡ Present address: Department of Zoology, University of British Columbia, Vancouver, British Columbia V6T 1Z4, Canada; e-mail: maughan@zoology.ubc.ca.

of  $N$  time steps of the Moran model, and so as  $N$  gets larger, the length of a time step decreases. The plasticity trait is subject to mutational loss at rate  $m$  per replication. Note that a complex trait may be lost through mutations at a range of loci, and so the functional mutation rate  $m$  may be considerably higher than a point mutation rate or even a per-gene mutation rate. A constant rate of mutational loss assumes that epistatic effects are not important in this context. This is consistent with data showing that an additional mutation has either the same (Elena and Lenski 1997; West et al. 1998; Elena 1999; Peters and Keightley 2000; Wloch et al. 2001) or a very similar (Bloom et al. 2005; Azevedo et al. 2006) effect in a mutationally loaded genetic background as it does in a wild-type background. Mutational loss may be accelerated by a selective advantage of loss  $s$  when there is a metabolic or other cost to maintaining the trait, although we can also set the cost  $s = 0$ . Using this Moran model with mutation, selection, and drift, we calculate in appendix A in the online edition of the *American Naturalist* the mean time  $\bar{\tau}$  for all individuals in the population to lose the trait in a static environment, given that they all have the trait initially. To avoid confusion with the time until trait loss in a fluctuating environment, we refer to the time  $\tau$  as the sojourn time, although it should be noted that this time includes the waiting time for the appearance of a mutant lacking the trait and also accounts for possible acceleration of trait loss due to the independent appearance of multiple mutants lacking the traits as part of a “soft sweep” (Hermisson and Pennings 2005).

Assume that environmental change events making the trait useful occur at rate  $\theta$  and occur according to a Poisson process. Assume that these events purge the population of all individuals not carrying the trait. The extreme nature of this assumption is addressed later in this article. Trait loss occurs if the waiting time until the next event is longer than the sojourn time  $\tau$ . Both of these are stochastic. As a Poisson process, the waiting time until the next event has an exponential distribution. No analytical expression exists for the probability distribution of the sojourn time (Ewens 2004), and so we calculate two tractable extreme cases, corresponding to very large and very small populations. Results for populations of intermediate size should fall between these two extreme scenarios. We verify this by computing expected times until trait loss numerically, which can be done without explicitly computing the distribution of sojourn times (see app. B in the online edition of the *American Naturalist*).

*Large-Population Approximation.* In the first scenario, we assume that populations are large so that  $mN \gg 1$ . In this case, sojourn times are highly deterministic, and we approximate variance in the sojourn time  $\tau$  as 0 (see app.

A). The constant sojourn time  $\tau = \bar{\tau}$  can be calculated as described in appendix A as a function of  $N$ ,  $m$ , and  $s$ . Since the waiting time until the next environmental change event has an exponential distribution, the probability that environmental change occurs before trait loss is then given by  $\int_0^{\bar{\tau}} \theta e^{-t\theta} dt = 1 - e^{-\theta\bar{\tau}}$ , purging the population of all genotypes that have lost the trait. The mean number of times this happens in succession is then  $(1 - e^{-\theta\bar{\tau}})/e^{-\theta\bar{\tau}}$ . The mean interval between environmental change events, given that trait loss does not occur, is

$$\frac{\int_0^{\bar{\tau}} t\theta e^{-t\theta} dt}{1 - e^{-\theta\bar{\tau}}} = \frac{e^{-\theta\bar{\tau}}(e^{\theta\bar{\tau}} - 1 - \theta\bar{\tau})}{\theta(1 - e^{-\theta\bar{\tau}})}.$$

The expected waiting time until trait loss occurs is given by the number of times that environmental change occurs before trait loss, multiplied by the mean interval time until environmental change on each of these occasions, plus the sojourn time after the last of these events, in which trait loss is not interrupted by environmental change. This can be expressed as

$$\frac{e^{\theta\bar{\tau}} - 1 - \theta\bar{\tau}}{\theta} + \bar{\tau} = \frac{e^{\theta\bar{\tau}} - 1}{\theta} \text{ generations.} \quad (1)$$

For a rarely used trait to be maintained, this number must be very large. For very small values of  $\theta$ , equation (1) gives approximately  $\bar{\tau}$ , which is unlikely to be sufficient for trait retention. For larger values of  $\theta$ , equation (1) increases approximately exponentially with  $\bar{\tau}$ . We now ask, For what parameter range is the waiting time until trait loss, as given by equation (1), greater than some large number of generations, taken here arbitrarily as  $10^8$ ? The exponentially steep character of equation (1) means that the precise arbitrary choice of  $10^8$  matters very little. For trait loss to take longer than  $10^8$  generations, we need

$$\bar{\tau} > \frac{\ln(10^8\theta + 1)}{\theta}. \quad (2)$$

The behavior of the cutoff value of  $\bar{\tau}$  is shown in figure 1. For sufficiently large values of  $\theta$ , this means that we need  $\bar{\tau} > \ln 10^8/\theta \approx 18/\theta$ . This captures the fact that environmental change must frequently interrupt trait loss. As environmental change gets rarer and  $\theta$  approaches the seemingly unrealistic value of  $10^{-8}$ , this requirement is relaxed in the direction of the looser requirement  $\bar{\tau} > \min(10^8, 1/\theta)$ .

*Small-Population Approximation.* In the second limiting scenario, we assume that populations are so small that  $mN \ll 1$ . In this case, the expected sojourn time has two

components: the expected waiting time until the first mutation destined for fixation, equal to  $1/m$  for the neutral case, and the expected subsequent time required for fixation, equal to  $N - 1$  in the neutral case. For  $mN \ll 1$ , the former component dominates.

Mutations destined for fixation appear according to a Poisson process. When  $N$  is sufficiently small, we can make the approximation that environmental change never interferes with the subsequent fixation process. Since the mean sojourn time of a neutral mutant destined for fixation is  $N - 1$ , a sufficient condition for this approximation to be accurate is  $\theta N \ll 1$ . When selection is also present, this condition is relaxed further.

With the small-population size approximation, trait loss events now occur at random points in time according to the same Poisson process that governs the appearance of mutations destined for fixation. In this case, the expected time until trait loss is independent of the environmental change rate and is given by  $\bar{\tau}$ , and so we need  $\bar{\tau} > 10^8$ . The waiting time until the next trait loss event has an exponential distribution with mean  $\bar{\tau}$ .

*Mean Sojourn Time for Populations of Any Size.* To interpret the approximate results for  $mN \gg 1$  and  $mN \ll 1$ , we need to know the value of  $\bar{\tau}$ . Exact formulas to calculate  $\bar{\tau}$  are derived in appendix A. In addition, the following approximate formula is derived as equation (A5) (in app. A):

$$\bar{\tau}_{\text{approx}} \approx \frac{1}{mNp_{\text{fix}}} + \begin{cases} \frac{\ln[(m+s)N] + \gamma}{m+s/2} & \ln[(m+s)N] > 0, \\ N-1 & \text{otherwise,} \end{cases} \quad (3)$$

where  $p_{\text{fix}}$  is the probability that a mutation present in a single individual will go on to become fixed and  $\gamma$  is Euler's constant, with numerical value 0.577216. In figure 2A and 2B, we show how  $\bar{\tau}$  depends on  $N$ ,  $m$ , and  $s$ , and in figure 2C, we see that the approximation is good over a wide range of parameter values. We see different behavior of  $\bar{\tau}$  in two distinct ranges for  $N$ . For small  $N$  with  $mN < 1$ , the sojourn time is dominated by the waiting time  $1/(mNp_{\text{fix}})$  until the appearance of the first mutant destined for fixation. For small enough  $N$  with  $sN \ll 1$ , this simplifies to  $1/m$ . As  $N$  increases within the  $mN < 1$  parameter range, then if  $s > m$ ,  $p_{\text{fix}}$  increases with  $N$  as selection becomes more effective, and so sojourn times decrease with  $N$ . If  $s < m$ , then the second parameter range begins before this effect becomes appreciable.

In the second parameter range of larger  $N$  with  $mN > 1$ , the sojourn time is dominated by the spread of mu-

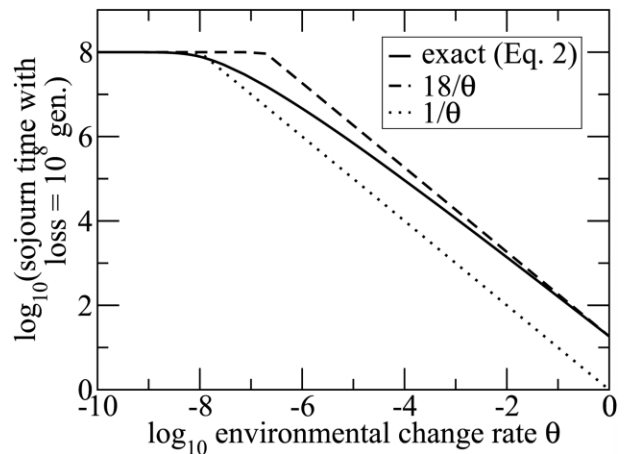
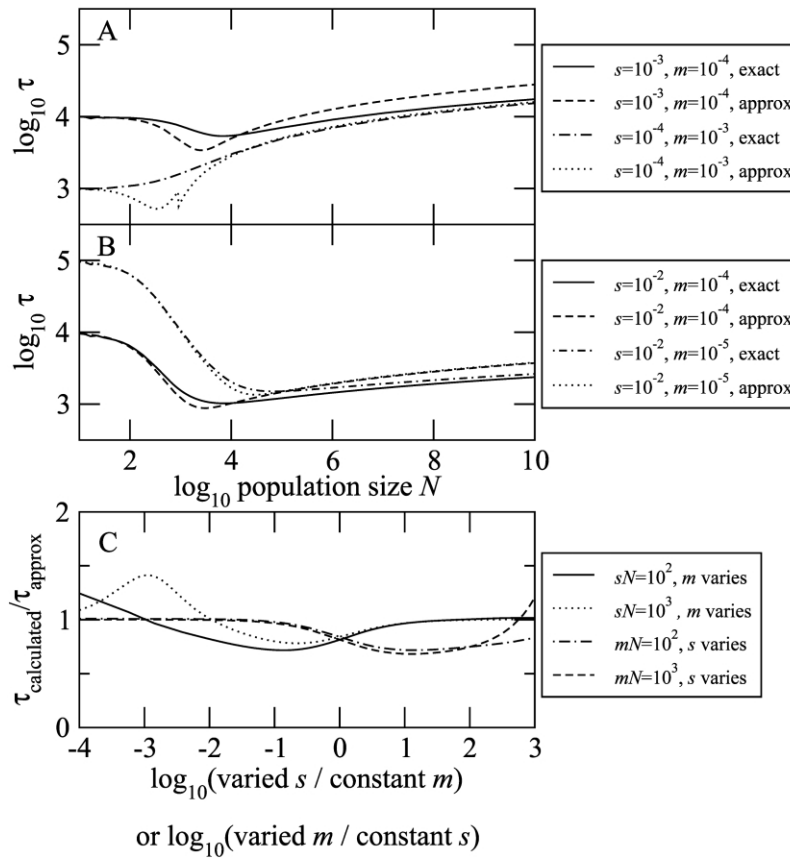


Figure 1: Minimum sojourn time required in order for trait loss in a single population to take an average of at least  $10^8$  generations in the large- $N$  (fixed- $\tau$ ) case, as a function of the frequency  $\theta$  with which environmental change purges the population of all individuals that have lost the trait. For large values of  $\theta$ , the trait is retained so long as  $\bar{\tau} > \ln 10^8/\theta \approx 18/\theta$ . For small values of  $\theta$ , this requirement is gradually weakened toward  $\bar{\tau} > \min(10^8, 1/\theta)$ .

tations through the population rather than by the time until the arrival of the first mutation. This arrests any decline in  $\bar{\tau}$  in the first parameter range and subsequently leads to a gentle increase in the sojourn time with  $N$ .

What sets the sojourn time in this second parameter range? Under neutral drift, conditional on fixation, the total sojourn time is equal to  $N - 1$  generations. Both selection and recurrent mutation as part of a soft sweep (Hermisson and Pennings 2005) can substantially accelerate this sojourn time, however. We see in equation (3) that for  $mN > 1$  and/or  $sN > 1$ , this acceleration can be captured by the term  $\{\ln[(m+s)N] + \gamma\}/(m+s/2)$ . Note that this term depends only weakly on  $N$  and is largely set by the value of  $1/(m+s/2)$ . If, instead, we have both  $mN \ll 1$  and  $sN \ll 1$ , then we have  $\bar{\tau} \approx 1/m$ .

*Comparison to Exact Solution.* In appendix B, we describe a method for calculating the mean time until trait loss that avoids the need for the approximations  $mN \gg 1$  or  $mN \ll 1$ . This method is shown schematically in figure 3. In figure 4, we test the conditions under which our previous approximations break down. We see that our large-population size approximation (given by eq. [2] and approximated still further in fig. 1 as  $\bar{\tau} > 18/\theta$ ) is sufficient whenever  $mN > 1$  and  $N \gg 1/\theta$ . Our small-population size approximation (the requirement that  $\bar{\tau} > 10^8$ ) is always sufficient and is necessary whenever  $N < 1/\theta$ . A smooth transition between the two approximate requirements is seen for intermediate values of  $N$ .



**Figure 2:** Mean sojourn time  $\bar{\tau}$  as a function of the population size  $N$ , the mutation rate  $m$ , and the selection coefficient  $s$ , as calculated exactly by equations (A1) and (A2) in the online edition of the *American Naturalist* and approximately by equation (3). A, B, We see differing behavior of  $\bar{\tau}$  depending on whether  $mN < 1$  or  $mN > 1$ . C, The approximate formula is reasonably accurate for a wide range of parameter values. Calculations shown were performed with  $N = 10^6$ .

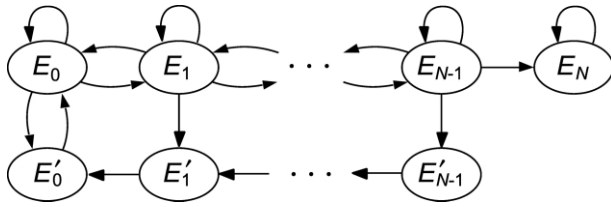
*Requirement to Avoid Trait Loss.* To integrate the calculations for  $\bar{\tau}$  with the requirements on  $\bar{\tau}$  for trait loss to be avoided, note from figure 4 that we need  $\bar{\tau} > 18/\theta$  for large  $N$ ,  $\bar{\tau} > 10^8$  for small  $N$ , and an intermediate requirement strongly dependent on the relationship between  $\bar{\tau}$  and  $1/\theta$  for intermediate values of  $N$ . The value of  $\bar{\tau}$  is dominated by the term  $\{\ln[(m+s)N] + \gamma\}/(m+s/2)$  in equation (3), particularly the denominator term  $1/(m+s/2)$ . In other words, to avoid trait loss, the sum of the mutation and selection coefficients must be small relative to the rate of environmental change, with the population size modifying the precise interpretation of “small.” When both  $mN \ll 1$  and  $sN \ll 1$ , the relevant approximation for  $\bar{\tau}$  becomes simply  $1/m$ .

#### Trait Loss from a Metapopulation

Consider a metapopulation in which environmental change occurs independently in each deme. In this sce-

nario, one deme may not encounter environmental change for a long period and therefore undergo trait loss. When the environment finally does change, this deme goes extinct. The extinct deme may, however, be recolonized by a different deme, which might, by chance, have experienced the event more regularly and hence maintained the trait. This rescue phenomenon may lead to persistence of the rarely used trait under a wider range of circumstances. In other cases, the extinct deme may be recolonized by a deme that lacks the trait; we assume that environmental change events represent episodes of selection rather than permanent changes.

We treat the metapopulation as a Markov process with  $j$  out of  $n$  demes lacking the trait. Environmental change events occur independently at rate  $\theta$  in each of the  $n$  demes, for a total rate of  $n\theta$ . When an environmental change event occurs in a deme that lacks the trait, then it is destroyed and recolonized from another deme chosen at random. This can sometimes lead to a decrease in the number of



**Figure 3:** State space of the Markov chain used for exactly computing the expected time until trait loss in a single population. States  $E_i$  and  $E'_i$  represent populations in which  $i$  of the  $N$  individuals lack the trait in the original and new environments, respectively. Edges between states indicate transitions that can happen in one step of the Markov chain, with probabilities given in appendix B. The chain begins in state  $E_0$ , and the trait is lost when the chain first reaches state  $E_N$ .

demes lacking the trait  $j$ ;  $j$  can also increase because of trait loss events within demes.

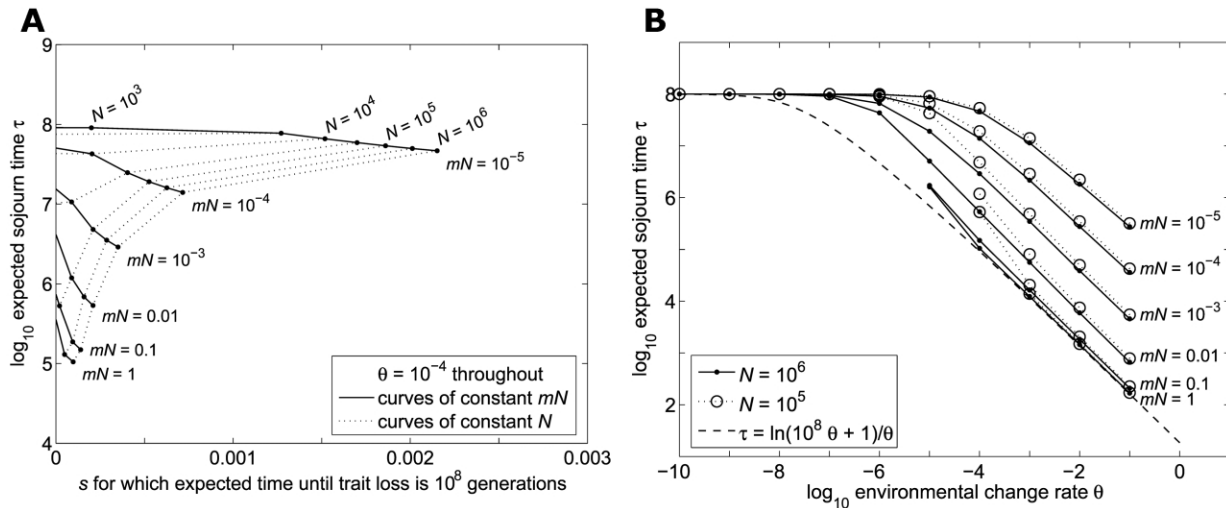
We consider two limiting cases. In the first, populations are small, trait loss occurs according to a Poisson process, and  $\tau$  therefore has an exponential distribution. In the second, populations are large, and hence  $\tau$  is constant. These two limiting cases are treated mathematically in appendixes C and D in the online edition of the *American Naturalist*, respectively. Both approximate analytic and exact simulated results are calculated when  $\tau$  is fixed as a constant.

In figure 5A, we plot the minimum number of demes needed to maintain the trait for an average of  $10^8$  generations, given  $\bar{\tau}$  and  $\theta$ . We see from the steep shape of the curves that beyond a very modest number of demes, the precise number of demes is not important. In figure 5B, we see that a trait can be maintained in a metapopulation of modest size so long as  $\bar{\tau} > 1.3/\theta$ . This expands the criterion  $\bar{\tau} > 18/\theta$  for trait retention in a single population around 15-fold in a metapopulation and perhaps slightly more for large population sizes with exponentially distributed  $\tau$ .

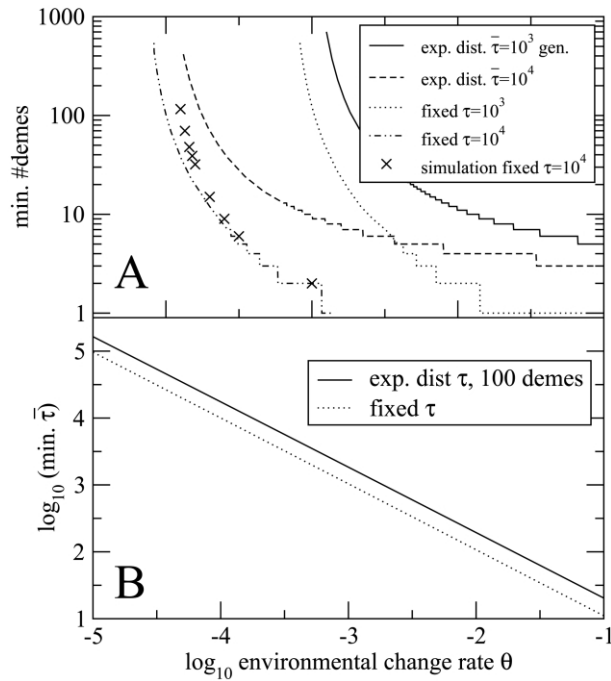
*Complete versus Partial Purging by Environmental Change*

To generate these results, we have assumed that when environmental change occurs, every last individual that lacks the trait is purged from the population. In a single population, the extreme nature of this assumption is primarily a mathematical convenience. Recurrent mutation means that individuals lacking the trait will in any case swiftly reappear, and so it is not likely to matter whether all individuals without the trait are purged or whether it is simply most that are purged.

In the metapopulation model, complete purging causes demes that lack the trait to go extinct and hence creates opportunities for new trait-bearing demes to be created



**Figure 4:** Exact computations of the time until trait loss in a single population. For a given  $\theta$ , the expected time until trait loss depends not just on  $\bar{\tau}$ —the expectation of the sojourn time  $\tau$ —but also on the distribution of  $\tau$ . For each plotted combination of  $\theta$ ,  $N$ , and  $m$ ,  $s$  was chosen so that the expected time until trait loss was exactly  $10^8$  generations (see app. B). The corresponding value of  $\bar{\tau}$  in shown on the vertical axes, computed as a function of  $N$ ,  $m$ , and  $s$ . In A,  $\theta$  is fixed at  $10^{-4}$ , and the values of  $s$  are explicitly shown. In B,  $\theta$  varies, but the values of  $s$  are not explicitly shown; points for which the corresponding value of  $s$  is negative are not shown, and so some curves are truncated as  $\theta$  decreases. Depending on  $\theta$ ,  $N$ , and  $m$ ,  $\bar{\tau}$  can range from the lower bound of  $\ln(10^8 \theta + 1)/\theta$  to the upper bound of  $10^8$ . Note that for fixed  $\theta$ , the mean sojourn time for which the expected time until trait loss is  $10^8$  generations tends to increase as  $mN$  decreases, as  $N$  decreases, and as  $s$  decreases; these are changes that tend to increase the variance of the sojourn time relative to its mean.



**Figure 5:** Conditions for trait loss to take longer than  $10^8$  generations in a metapopulation. A, Minimum number of demes needed as a function of  $\bar{\tau}$  and  $\theta$ . Equations (C1) and (C2) in appendix C are used for exponentially distributed sojourn times, equations (D1)–(D3) in appendix D are used for fixed sojourn times, and simulations are performed as described in appendix D. We see that there is little difference between the large- $N$  (fixed- $\tau$ ) and small- $N$  (exponentially distributed  $\tau$ ) curves unless the minimum number of demes is very small. B, By fitting a straight line of gradient  $-1$  to the curves shown, we calculate that the trait can be maintained with 100 demes so long as  $\bar{\tau} > 1.3/\theta$  for exponentially distributed  $\tau$  or  $\bar{\tau} > 1/\theta$  for fixed  $\tau$ . The simulation results in A suggest that the true cutoff for exponentially distributed  $\tau$  may also be closer to  $\bar{\tau} > 1.3/\theta$ , and so this conservative criterion is used throughout. This criterion is fairly insensitive to the precise number of demes; for example, for 50 demes, the criterion for exponentially distributed  $\tau$  is  $\bar{\tau} > 1.5/\theta$ .

through colonization. The results of the model should be robust so long as environmental change causes a highly elevated probability of deme replacement. For example, pathogens encounter a fluctuating environment with frequent “adapt or die” dynamics. Under these circumstances, all demes turn over as the environment keeps shifting, and the model is a good description.

#### Quantitative Roles of Mutation and Selection in Trait Loss

Note the partial symmetry between parameters  $m$  and  $s$  in equation (3). This symmetry is weakest for small populations: when both  $mN \ll 1$  and  $sN \ll 1$ , then  $m$  and  $N$  alone set the value of  $\bar{\tau}$ , irrespective of whether  $m > s$ . For large populations with both  $mN \gg 1$  and  $sN \gg 1$ , the sym-

metry is not obvious a priori: in particular,  $m$  will have a larger effect than  $s$  when individuals lacking the trait are rare. Nevertheless, the close fit shown in figure 2 between the exact and approximate solutions shows that the effects of  $m$  and  $s$  are close to symmetric in practice in large populations.

This symmetry means that in larger populations with  $mN > 1$  and/or  $sN > 1$ , trait loss is primarily driven by the larger of  $s$  and  $m$ . Mutation rates are normally thought of as small, but note that the parameter  $m$  refers to the functional mutation rate, which may be the sum of many possible mutations over multiple genes. Data on functional mutation rates are sparse, but one study on loss of sporulation ability in *Bacillus subtilis* gives  $m = 0.0003$  in non-mutator strains (Masel and Maughan 2007). Data on gene deletions in yeast suggest that, in most cases,  $s < 0.005$  (Sliwa and Korona 2005).

Mutational degradation of the ability to switch between adaptively plastic phenotypes may occur through damage to the switching mechanism itself, or it may cause the switch to reveal lethal variation that was hidden in the “off” state (Masel 2006). Either way, the ability to switch is effectively eroded. In the former case, there is likely to be a selective advantage to trait loss, because inappropriate switching events are minimized. In the latter case, however, there is unlikely to be a selective advantage to trait loss, and there may even be a slight selective penalty.

Note that if estimates or bounds on  $m$  and  $s$  are available, we can infer the minimum rate  $\theta$  of environmental change required to explain the fact that an observed adaptively plastic trait persists. For example, the yeast prion  $[PSI^+]$  appears spontaneously at a rate of about  $10^{-7}$  to  $10^{-5}$  per replication (Lund and Cox 1981; Liu and Lindquist 1999; Nakayashiki et al. 2001) and is likely deleterious on these occasions (Nakayashiki et al. 2005). Yeast have effective population size  $N_e \approx 10^8$  (Lynch and Conery 2003; Wagner 2005). If we assume a mutational degradation rate  $m < 0.0003$  and selection  $s < 10^{-6}$  against inappropriate appearance of the prion, then for the ability to form prions to persist, we need  $\bar{\tau} > 1.3/\theta$ . Using our bounds, we calculate  $\bar{\tau} > \bar{\tau}(N = 10^8; m = 0.0003; s = 10^{-6}) = 36,200$  generations according to the exact methods given in equations (A1) and (A2) (in app. A), yielding the condition  $\theta > 3.6 \times 10^{-5}$  as sufficient for persistence. This value of  $\theta$  corresponds to environmental changes that favor the trait occurring every  $1/\theta = 28,000$  generations, on average. With such a low value of  $\theta$  needed, the inability to catch  $[PSI^+]$  “in the act” (Nakayashiki et al. 2005) is insufficient evidence that rare selection events are not responsible for the maintenance of the ability to form  $[PSI^+]$ .

*Different Forms of Weak Selection*

How does strong but rarely applied selection compare to constant but weak selection in the context of trait loss? Weakly advantageous selection for trait retention can be represented in our model by setting  $s$  to a negative value. To obtain a comparable scenario with constant weak selection, we take the strong, rare selection studied here so far and “spread it out” over time by setting  $s$  equal to  $-\theta$  and then calculating the sojourn time for a single population with no environmental change.

This case of positive selection and mutational degradation as opposing forces has been described in detail elsewhere, in work showing that trait loss can sometimes be so rapid that it occurs even before a novel sequence has fixed in the population (Berg and Kurland 2002). For trait retention rather than fixation (i.e., expected time until trait loss  $> 10^8$  generations), we find, unsurprisingly, that we need  $-s > m$ ; that is, selection must be stronger than mutation. This criterion is similar to the corresponding criterion for rarely used traits. A second, additional criterion for constant weak selection, however, is that we need  $-s > 1/N$ . Considering a metapopulation rather than a single population does not significantly weaken this second criterion, which is based on the population size within a deme.

This criterion has no correspondent in the case of a rarely used trait. In other words, rarely applied but strong selection to a modest number of small demes can be effective even when the same selective force, made constant by being averaged out, is not effective. This is because the total frequency of selective events in a metapopulation is given by  $n\theta$  and hence scales linearly with the total population size of the metapopulation, while with constant selection, the sojourn timescales only very weakly with the logarithm of  $N$ . For this reason, the population size makes surprisingly little difference to the retention of a rarely used trait.

*Population Extinction*

If the trait is lost, will this cause population extinction? As the model is formulated so far, recolonization of lost demes is instant. Even once all demes have lost the trait, demes go extinct one at a time, since environmental change is not synchronized. Rapid recolonization follows each deme loss event, and so population extinction will never occur in a metapopulation.

Relaxing this, let  $\beta$  be the rate at which a deme sends out emigrants, and so the number of migrants able to settle is  $\beta k$ , where  $k$  is the number of demes occupied out of a maximum of  $n$ . The probability that a migrant settles in an empty deme and is therefore able to colonize it is

$(1 - k/n)$ , and so the total rate of recolonization is  $\beta k(1 - k/n)$ . Now the criterion for population persistence is  $\beta > \theta$ , according to the standard criterion for persistence in a deterministic Levins’s model (Levins 1969). In a stochastic setting, this criterion remains sound for modest minimum values of  $n$  (Gurney and Nisbet 1978; reviewed by Hanski et al. [1996]; see Alonso and McKane 2002 for extension to mainland island metapopulations).

Previous work studied trait loss within demes as well as deme extinction and calculated the proportion of remaining demes that retain the trait (Wagner 2003). The conclusions were in agreement with results for infinite populations (Wagner 2003). Although this work allowed for the extinction of individual demes, it did not allow for the extinction either of the trait within the metapopulation or of the metapopulation itself (Wagner 2003).

Here we have taken treatment of extinction further by explicitly including extinction processes at the metapopulation level. We have calculated the parameter regime required for negligibly slow processes of both trait loss within an entire metapopulation and extinction of the metapopulation itself.

**Discussion***Data on Mutational Degradation*

Here we have considered whether mutational degradation can be a powerful enough force to override the selective benefits of a rarely needed trait. Mutational degradation of a complex switching trait is likely to occur at a much higher rate than its restoration by compensatory mutations. In practice, mutational degradation of sporulation has been observed in the laboratory in as few as 4,200–6,000 generations (H. Maughan, J. Masel, C. W. Birky, and W. L. Nicholson, unpublished manuscript). This is consistent with observations from natural populations of bacteria, where studies of whole bacterial genomes support the notion that traits are frequently lost throughout evolutionary time, especially in species that have colonized relatively constant environments (reviewed in Bentley and Parkhill 2004).

The relationship between environmental change and functional degradation is also supported by genome size data. In bacteria, genome size is a good indicator of the frequency of environmental change because more genes are needed to deal with the various environments that are encountered. Genomes of soil bacteria, which encounter frequent environmental change, are notoriously large, while genomes of obligate endosymbiotic bacteria, which live in a comparatively static host environment, are invariably small (reviewed in Bentley and Parkhill 2004). Genome degradation under such static environments is

likely due to deletional biases in bacterial genomes (Mira et al. 2001), where genes that are not under selection are degraded and ultimately lost from the genome.

#### *Persistence across Time versus Space*

Here we have considered the question of whether the ability to switch between alternative strategies can be maintained in the face of mutational degradation. Our results can be interpreted as a statement of the parameter range for which retained alternative strategies persist in a spatial and/or a temporal context (Venable and Lawlor 1980). When a rarely used trait is retained in a single population, this constitutes persistence across time. This occurs when  $\bar{\tau} > 18/\theta$ , for  $mN > 1$  and  $N\theta \gg 1$ , or when  $\bar{\tau} > 10^8$ . When a rarely used trait is retained only in the context of a metapopulation, this constitutes persistence over time that relies on interaction with persistence across space. This occurs when the above condition is not met but  $\bar{\tau} > 1.3/\theta$ . When the trait is lost but the population nevertheless persists within a metapopulation context, this corresponds to persistence across space alone. This occurs when  $\bar{\tau} < 1.3/\theta$  and  $\beta > \theta$ . Finally, when none of these apply, the population becomes extinct.

#### *Trade-Offs*

Evolutionary biology is often about identifying the appropriate trade-off(s). Switching phenomena have been seen as a trade-off between inappropriate switching, failing to switch when necessary, and the metabolic costs of sensing when to switch (Kussell and Leibler 2005). This falls in the most common evolutionary biology tradition of identifying trade-offs between selection for the benefits of a trait and selection against the costs, with a solution found using geometric mean fitness calculations. Another well-understood form of trade-off is between selection for benefits and stochasticity associated with genetic drift in a finite population. The well-known solution to this trade-off is that selection is stronger than drift so long as  $s > 1/N$ .

Here we have solved for another distinct trade-off: that associated with stochasticity in the timing of events rather than stochasticity associated with the finiteness of a population. This is relevant for recent models of switching phenomena that have emphasized precisely these very rare environmental shifts, such that the dynamics of allele frequencies following an environmental change are rapid relative to the intervals between environmental changes (Masel and Bergman 2003; Kussell and Leibler 2005; Masel 2005).

We have analyzed the trade-off between selection for benefits and irreversible drift in the long intervals between

rare selection events. We have found that the results depend surprisingly little on the population size but instead depend on the relative magnitude of mutation and selection coefficients eroding the adaptively plastic trait versus the frequency of environmental change events that cause the benefits of the trait to be selected. Note that although the population size does not appear explicitly in this condition, it nevertheless applies only to a finite population. This is because extinction of alleles never occurs in a truly infinite population. In practice, however, the sojourn time until extinction depends only mildly on the population size, and so no population is ever large enough to be accurately approximated as infinite.

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#### **Literature Cited**

- Abraham, J. M., C. S. Freitag, J. R. Clements, and B. I. Eisenstein. 1985. An invertible element of DNA controls phase variation of type-1 fimbriae of *Escherichia coli*. Proceedings of the National Academy of Sciences of the USA 82:5724–5727.
- Alonso, D., and A. McKane. 2002. Extinction dynamics in mainland-island metapopulations: an  $N$ -patch stochastic model. Bulletin of Mathematical Biology 64:913–958.
- Azevedo, R. B. R., R. Lohaus, S. Srinivasan, K. K. Dang, and C. L. Burch. 2006. Sexual reproduction selects for robustness and negative epistasis in artificial gene networks. Nature 440:87.
- Balaban, N. Q., J. Merrin, R. Chait, L. Kowalik, and S. Leibler. 2004. Bacterial persistence as a phenotypic switch. Science 305:1622–1625.
- Bentley, S. D., and J. Parkhill. 2004. Comparative genomic structure of prokaryotes. Annual Review of Genetics 38:771–792.
- Berg, O. G., and C. G. Kurland. 2002. Evolution of microbial genomes: sequence acquisition and loss. Molecular Biology and Evolution 19:2265–2276.
- Bloom, J. D., J. J. Silberg, C. O. Wilke, D. A. Drummond, C. Adami, and F. H. Arnold. 2005. Thermodynamic prediction of protein neutrality. Proceedings of the National Academy of Sciences of the USA 102:606–611.
- Elena, S. F. 1999. Little evidence for synergism among deleterious mutations in a nonsegmented RNA virus. Journal of Molecular Evolution 49:703–707.
- Elena, S. F., and R. E. Lenski. 1997. Test of synergistic interactions among deleterious mutations in bacteria. Nature 390:395–398.
- Ewens, W. J. 2004. Mathematical population genetics. I. Theoretical introduction. Springer, New York.
- Gurney, W. S. C., and R. M. Nisbet. 1978. Single-species population fluctuations in patchy environments. American Naturalist 112: 1075–1090.

- Hallet, B. 2001. Playing Dr. Jekyll and Mr. Hyde: combined mechanisms of phase variation in bacteria. *Current Opinion in Microbiology* 4:570–581.
- Hanski, I., A. Moilanen, and M. Gyllenberg. 1996. Minimum viable metapopulation size. *American Naturalist* 147:527–541.
- Henderson, I. R., P. Owen, and J. P. Nataro. 1999. Molecular switches: the ON and OFF of bacterial phase variation. *Molecular Microbiology* 33:919–932.
- Hermisson, J., and P. S. Pennings. 2005. Soft sweeps: molecular population genetics of adaptation from standing genetic variation. *Genetics* 169:2335–2352.
- Kussell, E., and S. Leibler. 2005. Phenotypic diversity, population growth, and information in fluctuating environments. *Science* 309:2075–2078.
- Levins, R. 1969. Some demographic and genetic consequences of environmental heterogeneity for biological control. *Bulletin of the Entomology Society of America* 71:237–240.
- Liu, J. J., and S. Lindquist. 1999. Oligopeptide-repeat expansions modulate “protein-only” inheritance in yeast. *Nature* 400:573–576.
- Lund, P. M., and B. S. Cox. 1981. Reversion analysis of [*psi*<sup>-</sup>] mutations in *Saccharomyces cerevisiae*. *Genetical Research* 37:173–182.
- Lynch, M., and J. S. Conery. 2003. The origins of genome complexity. *Science* 302:1401–1404.
- Masel, J. 2005. Evolutionary capacitance may be favored by natural selection. *Genetics* 170:1359–1371.
- . 2006. Cryptic genetic variation is enriched for potential adaptations. *Genetics* 172:1985–1991.
- Masel, J., and A. Bergman. 2003. The evolution of the evolvability properties of the yeast prion [*PSI*<sup>+</sup>]. *Evolution* 57:1498–1512.
- Masel, J., and H. Maughan. 2007. Mutations leading to loss of sporulation in *Bacillus subtilis* are sufficiently frequent to favor genetic canalization. *Genetics* (forthcoming), doi: 10.1534/genetics.106.065201.
- Mira, A., H. Ochman, and N. A. Moran. 2001. Deletional bias and the evolution of bacterial genomes. *Trends in Genetics* 17:589–596.
- Nakayashiki, T., K. Ebihara, H. Bannai, and Y. Nakamura. 2001. Yeast [*PSI*<sup>+</sup>] “prions” that are cross-transmissible and susceptible beyond a species barrier through a quasi-prion state. *Molecular Cell* 7:1121–1130.
- Nakayashiki, T., C. P. Kurtzman, H. K. Edsles, and R. B. Wickner. 2005. Yeast prions [*URE3*] and [*PSI*<sup>+</sup>] are diseases. *Proceedings of the National Academy of Sciences of the USA* 102:10575–10580.
- Peters, A. D., and P. D. Keightley. 2000. A test for epistasis among induced mutations in *Caenorhabditis elegans*. *Genetics* 156:1635–1647.
- Sliwa, P., and R. Korona. 2005. Loss of dispensable genes is not adaptive in yeast. *Proceedings of the National Academy of Sciences of the USA* 102:17670–17674.
- Sumby, P., and M. C. M. Smith. 2003. Phase variation in the phage growth limitation system of *Streptomyces coelicolor* A3(2). *Journal of Bacteriology* 185:4558–4563.
- True, H. L., and S. L. Lindquist. 2000. A yeast prion provides a mechanism for genetic variation and phenotypic diversity. *Nature* 407:477–483.
- Venable, D. L., and L. Lawlor. 1980. Delayed germination and dispersal in desert annuals: escape in space and time. *Oecologia (Berlin)* 46:272–282.
- Wagner, A. 2003. Risk management in biological evolution. *Journal of Theoretical Biology* 225:45–57.
- . 2005. Energy constraints on the evolution of gene expression. *Molecular Biology and Evolution* 22:1365–1374.
- West, S. A., A. D. Peters, and N. H. Barton. 1998. Testing for epistasis between deleterious mutations. *Genetics* 149:435–444.
- West-Eberhard, M. J. 2003. *Developmental plasticity and evolution*. Oxford University Press, Oxford.
- Wloch, D. M., R. H. Borts, and R. Korona. 2001. Epistatic interactions of spontaneous mutations in haploid strains of the yeast *Saccharomyces cerevisiae*. *Journal of Evolutionary Biology* 14:310–316.

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